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Paper Code : OM 403 OPERATIONS RESEARCH APPLICATIONS

UPID : 004684

Time Allotted : 3 Hours

Full Marks : 70

The Figures in the margin indicate full marks.

Candidate are required to give their answers in their own words as far as practicable

Group-A (Very Short Answer Type Question)

1. Answer any ten of the following :

[1 x 10 = 10]

- (I) What indicates a zero element in the transition matrix?
- (II) Give an example of a dynamic queue discipline.
- (III) How many number of iteration usually required solving a LP problem with n number of constraints?
- (IV) The optimal value of the objective function is same for the primal and _____ problem.
- (V) Write the names of two methods for solving integer programming problems.
- (VI) What are some examples of non-linear programming models?
- (VII) What types of problems can be solved using dynamic programming?
- (VIII) In the optimal simplex table, if there exists alternative solution then what will be the value of $c_j - z_j$?
- (IX) What is a feasible solution in integer linear programming?
- (X) What are the key components of operation research?
- (XI) When a calling population is considered to be infinite?
- (XII) What represents a stage in a dynamic programming problem?

Group-B (Short Answer Type Question)

Answer any three of the following :

[5 x 3 = 15]

2. How does a quadratic programming problem differ from a linear programming problem? [5]
3. Discuss applications of linear programming. [5]
4. What do you understand by queue discipline? [5]
5. Explain and graphically illustrate in-feasibility and un-boundedness. [5]
6. In which conditions the Markov chain reaches the steady-state equilibrium? [5]

Group-C (Long Answer Type Question)

Answer any three of the following :

[15 x 3 = 45]

7. (a) Why we need non-linear programming models? [5]
 (b) Solve graphically the following non-linear programming problem: [10]

$$\text{Max } Z = 2x_1 + 3x_2$$
 Subject to the constraints
 (i) $x_1^2 + x_2^2 \leq 20$,
 (ii) $x_1 \cdot x_2 \leq 8$,
 and $x_1, x_2 \geq 0$.
8. (a) What are the advantages and disadvantages of the simplex method? [7]
 (b) Use Simplex Method to solve the following L.P.P. : [8]

$$\text{Max } Z = 4x_1 + 10x_2$$
 Subject to solve the constraints:
 $2x_1 + x_2 \leq 50$,
 $2x_1 + 5x_2 \leq 100$,
 $2x_1 + 3x_2 \leq 90$,
 $x_1 \geq 0$ and $x_2 \geq 0$.
9. (a) What is the meaning and the role of the lower bound and upper bound in the Branch and Bound method? [9]
 (b) Discuss any one method to solve integer programming problem. [6]

10. In a railway marshalling yard, goods trains arrive at a rate of 30 trains per day. Assuming that the inter-arrival time follows exponential distribution and service time distribution is also exponential with an average 36 minutes. Calculate the following: [15]
- (i) The mean queue size (line length), and
 - (ii) The probability that the queue size exceeds 10.
 - (iii) If the input of trains increases to an average 33 per day, what will be the change in (i) and (ii).

11. Solve the following LP problem by dynamic programming approach: [15]

$$\text{Max } Z = 8x_1 + 7x_2$$

Subject to the constraints

(i) $2x_1 + x_2 \leq 8$,

(ii) $5x_1 + 2x_2 \leq 15$,

and $x_1, x_2 \geq 0$.

*** END OF PAPER ***